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Abstract. A theoretical model that deals with SHG from crystallized type I collagen fiber formed by a bundle of fibrils is established. By introducing a density distribution function of dipoles within fibrils assembly into the dipole theory and combining with structural order (m,l) parameters revealed by quasi-phase-matching (QPM) theory, our established theoretical model comprehensively characterizes both biophysical features of collagen dipoles and the crystalline characteristics of collagen fiber. This new model quantitatively reveals the 3-D distribution of second-harmonic generation (SHG) emission angle (θ,φ) in accordance with the emission power. Results show that fibrils diameter d_1 and structural order m , which describes the structural characteristics of collagen fiber along the incident light propagation direction has significant influence on backward/forward SHG emission. The decrease of fibrils diameter d_1 induces an increase of the peak SHG emission angle θ_{\max} . As d_1 decreases to a threshold value, in our case it is around $d_1 = 150$ nm when $(m,l) = (1,0)$, $\theta_{\max} > 90$ deg, indicating that backward SHG emission appears. The SHG may have two symmetrical emission distribution lobes or may have only one or two unsymmetrical emission lobes with unequal emission power, depending on the functional area of (m,l) on d_1 . © 2011 Society of Photo-Optical Instrumentation Engineers (SPIE). [DOI: 10.1117/1.3596174]

Keywords: crystallized collagen fibers; microscopic second-harmonic generation; backward emission angle.

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1 Introduction

Second-harmonic microscopy, a microscopic technique taking advantage of second harmonic generation (SHG) signals, has been proved to be an effective tool for biological tissues imaging especially for type I collagen fiber visualization.¹⁻⁵ Highly organized by a bundle of closely packed thin fibrils, type I collagen fiber has been experimentally verified that it has quasi-crystalline structure features.^{6,7} Those constituted fibrils have cylindrical shape with a diameter varying from 10 to 500 nm (mean diameter of 40–80 nm) relying on the locations of the tissues as well as the age and species of animals.⁸

Collagen type I fiber is the excellent intrinsic biomedical material for SHG, and microscopic SHG signals emitted from collagen fiber have been exploited for application into enormous areas. As the fiber polymerization or degradation evolves parallel with the evolution of normal physiological development or pathological conditions, SHG microscopy offers an effective means of characterizing collagen in development, distinguishing different collagen types, and identifying degradation of collagen in various pathological conditions and diseases, such as wound healing and malignancy.⁹⁻¹¹ Very recently, by use of the polarization-sensitive feature of SHG, polarization SHG (PSHG) microscopy has been used to characterize the tissues,

such as collagen and muscle as well as axon, by distinguishing their SHG characteristic angles, the effective (or apparent) angle corresponding to the most probable orientation of the active molecules.¹²⁻¹⁴ The effective angles for collagen and muscle are respectively correlated to the helical pitch angle of one polypeptide chain of the collagen triple-helix and the α -helix of the myosin's coiled coil (myosin tail).

A large number of experiments of microscopic SHG thus far are confirmed to be done by backward collection geometry; however, appreciable backward SHG emissions from collagen type I were observed.¹⁵⁻¹⁸ This phenomenon looks like it contradicts the SHG coherent process, because normally, only in the same forward-going direction, could the extended scatterers synchronously emit with a forward-going fundamental wave to remain phase matched. The investigation of the role of backscattering of SHG reveals that backscattered SHG signals account for only a small fraction of total backward SHG signals,¹⁸ suggesting the presence of other generation mechanisms of the prominent backward SHG, except the backscattering. However, in many cases in practice, such as *in vivo* and *ex vivo* thick tissue imaging, backward detection is required because, under such conditions, collecting the forward-propagating signals is almost impractical. Hence, in this case, to establish the theoretical model to explore the creation mechanism of the initial backward SHG signal is significant both physically and practically.

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Theoretical models to explore the generation of SHG signals from type I collagen fiber have been extensively established, but most of them target single hypothetical fibrils composed of dipoles;^{16,19} no backward emission issue is thus involved. Until recently, the investigators started to deal with collagen fiber as a multiple-fibril assembly by use of quasi-phase-matching (QPM) theory.²⁰ With the framework of this theory,^{21,22} we could analyze the SHG emission angle and its relevant influential factors.²³ Nevertheless, this revealed angle is the most possible emission angle of SHG, not the emission angle distribution with emission power; thus, it is a two-dimensional presentation. Also, the biophysical feature of the constituted collagen dipoles in the fibrils is incapable of being reflected in this theory. In this paper, a more comprehensive theory that covers the biophysical feature of the constituted dipoles within fibrils assembly by introducing a density distribution function of dipoles into the dipole theory and, simultaneously, the structural characteristics of crystallized collagen fiber described by QPM theory will be established. With this model, the three-dimensional distribution of an SHG emission angle in accordance with emission power could be sufficiently explored, our quantitative study of SHG backward emission angle thus could be thoroughly carried on.

2 Theory of Microscopic Second Harmonic Generation from Crystallized Collagen Fiber

Figure 1(a) demonstrates our particular model for dealing with SHG emission from the crystallized collagen fiber at an observation point (r, θ, φ) under the specific coordinate system. The crystallized collagen fiber is assumed to be constituted by a bundle of closely packed thin fibrils, which highly organize along the \bar{x} -axis and form a 2-D crystalline structure in its cross section. The fibrils are supposed to have the diameter of d_1 , and the interspaces filled by water have the distance of d_2 . Accordingly, the Bravais lattice, exhibiting crystalline structure formed by fibrils, can be determined by the position vector $\vec{R} = \vec{D}_1 + \vec{D}_2$, where \vec{D}_1, \vec{D}_2 are the primitive vectors that denote two directions as \vec{z}, \vec{y} , respectively. We further define $D_1 = D_2 = d_1 + d_2 = D$ in our case, which indicates a square Bravais lattice

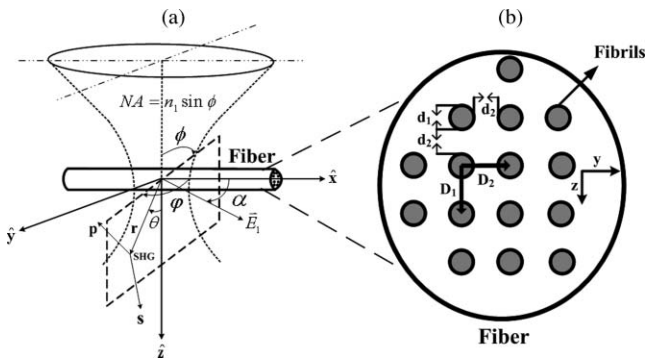


Fig. 1 (a) Schematic diagram of the model of focused light on fiber for SHG emission. The light with the linear polarization angle α from \bar{x} -axis is focused by the objective with numerical aperture $NA = n_1 \sin \phi$ (where ϕ is the incident angle of the focused light and n_1 is the refractive index of collagen at the fundamental wavelength λ_1). The emission SHG is shown by polar coordinates (r, θ, φ) . (b) Quasi-crystalline structural model of type I collagen fiber.

as shown in Fig. 1(b). The fibrils are regarded to be composed of dipoles that have uniform density.

The excitation laser light with linear polarization angle α from \bar{x} direction on the collagen fibrils bundle is assumed to be focused by a microscopic objective, which has the numerical aperture $NA = n_1 \sin \phi$, where ϕ is the incident angle of the focused beam and n_1 is the refractive index of collagen at the fundamental wavelength λ_1 .

2.1 Fundamental Field \vec{E}_1

For the focused condition, the \vec{z} -directed beam at the focus can be well approximated as follows:

$$\vec{E}_1(x, y, z) = -iE_1^{(0)} \exp \left(-\frac{\bar{x}^2 + \bar{y}^2}{\omega_{xy}^2} - \frac{\bar{z}^2}{\omega_z^2} + i\xi k_1 \bar{z} \right), \quad (1)$$

where $E_1^{(0)}$ is the amplitude of the fundamental field at the point $(x, y, z) = (0, 0, 0)$. ξk_1 is the Guoy phase shift due to focusing, which causes a phase retardation of the light near the focus center along the axial direction and, thus, accordingly induces a decrease of the axial momentum k_1 [$k_1 = (2\pi/\lambda)n_1$ is the wave vector of the fundamental wave λ_1] to be ξk_1 by a reduction factor $\xi < 1$. The relationship of ξ to NA can be approximately described as follows:¹⁶

$$\xi \approx \cos \left[\sin^{-1} \left(\frac{NA}{n_1} \right) / \sqrt{2} \right] \quad (\text{when } NA < 1.2, \text{ at most}), \quad (2)$$

where ω_{xy} and ω_z are the transversal and axial beam amplitude profiles, respectively, which restrict the SHG formation in the excitation areas,²⁴

$$\omega_{xy} = \frac{0.320\lambda_1}{\sqrt{2}NA} \quad (NA \leq 0.7), \quad \omega_{xy} = \frac{0.325\lambda_1}{\sqrt{2}NA^{0.91}} \quad (NA > 0.7),$$

$$\omega_z = \frac{0.532\lambda_1}{\sqrt{2}} \left[\frac{1}{n_1 - \sqrt{n_1^2 - NA^2}} \right]. \quad (3)$$

2.2 Induced Second Harmonic Generation Dipole Moment

A Taylor series of the dipole moment $\vec{\mu}$, which is induced by the field \vec{E}_1 , is

$$\vec{\mu} = \vec{\mu}_0 + \alpha \cdot \vec{E}_1 + \frac{1}{2!} \beta \cdot \vec{E}_1^2 + \frac{1}{3!} \gamma \cdot \vec{E}_1^3 + \dots$$

The SHG is related to the first hyperpolarizability term β , the third term $(1/2!) \beta \cdot \vec{E}_1^2$. Thus, the total local dipole moment can be expressed as

$$\vec{\mu}_{2,i}(x, y, z) = \frac{1}{2} \vec{E}_1^2(x, y, z) \sum_{j,k} \langle \beta_{ijk} \rangle \hat{e}_j \hat{e}_k, \quad (4)$$

where \hat{e}_j and \hat{e}_k is the unit vector along the direction of $j(\hat{x}, \hat{y}, \hat{z})$ and $k(\hat{x}, \hat{y}, \hat{z})$ directions, respectively.

According to the assumption of Kleinman and cylindrical symmetry, a linearly polarized beam at an angle α , as shown in

Fig. 1, produces the following SHG dipole moment:¹⁹

$$\begin{aligned}\bar{\mu}_2(x, y, z) &= \frac{1}{2} \bar{E}_1^2(x, y, z) \begin{pmatrix} \beta_{xxx} \cos^2 \alpha + \beta_{xyy} \sin^2 \alpha \\ \beta_{xyy} \sin 2\alpha \\ 0 \end{pmatrix} \\ &= \frac{1}{2} \bar{E}_1^2(x, y, z) \beta.\end{aligned}\quad (5)$$

2.3 Induced Second Harmonic Generation Electric Field from Single Dipole

The configuration of induced electrical field of SHG far from the dipole is²⁵

$$\bar{E}_2(\psi) = \frac{\bar{\mu}_2 \omega^2}{\pi \epsilon_0 c^2 r} \sin(\psi) \exp(-i \bar{k}_2 \cdot \bar{r}) \bar{\psi}, \quad (6)$$

where ψ represents the angle between \bar{x} -axis and the emission direction \bar{r} of SHG. The projection relationship between the excitation electric field \bar{E}_2 of SHG and the direction of emission SHG dipole moment $\bar{\mu}_2$ is $\sin \psi = (\sin^2 \theta \sin^2 \varphi + \cos^2 \theta)^{1/2}$. And ω is the frequency of fundamental beam, ϵ_0 is the sprec-space permittivity, and c is the speed of light. We define $\nu = \omega^2 / \pi \epsilon_0 c^2$ here.

2.4 Induced Electric Field of Second Harmonic Generation from Crystallized Collagen Fiber

The total radiated second-harmonic signals from the collagen fibrils bundle are the integration from all scatterers (dipoles). We assume that the collagen dipoles, which distribute in crystalline structure of fiber with fibrils assembly, have a spatially heterogeneous concentration $C(x, y, z)$ and the volume density of uniform distribution of dipoles in fibrils is C_v . The emitted \bar{E}_2 of SHG is thus described as follows:

$$\begin{aligned}\bar{E}_2(\theta, \varphi) &= \frac{\nu}{r} \iiint \sin \psi \cdot \bar{\mu}_2(x, y, z) \cdot C(x, y, z) \\ &\quad \times \exp[-i k_2(z \cos \theta + y \sin \theta \sin \varphi \\ &\quad + x \sin \theta \cos \varphi)] dx dy dz\end{aligned}$$

According to the model in Fig. 1, the Fourier transform of $C(x, y, z)$ is

$$C(x, y, z) = C_v \sum_{m, l} G_{ml} \exp(-i \bar{K}_{ml} \cdot \bar{r}) \quad (7)$$

where

$$G_{ml} = \frac{2d_1}{D\sqrt{m^2 + l^2}} J_1 \left(\frac{2\pi}{D} d_1 \sqrt{m^2 + l^2} \right)$$

and $J_1(x)$ is Bessel function. On the basis of the QPM theory,²² the periodical structure of collagen fibrils bundle causes an additional wave vector \bar{K}_{ml} , which is

$$\bar{K}_{ml} = \frac{2\pi m}{D} \bar{z} + \frac{2\pi l}{D} \bar{y} \quad (8)$$

where m and l are positive integers that represent the structural order (m, l) of \bar{K}_{ml} in the direction of \bar{z} and \bar{y} respectively, as

shown in Fig. 1(b). Therefore,

$$\begin{aligned}\bar{E}_2(\theta, \varphi) &= \sum_{m, l} \frac{\nu C_v}{r} (\sin^2 \theta \sin^2 \varphi + \cos^2 \theta)^{1/2} \iiint \frac{1}{2} \beta G_{ml} \bar{E}_1^{(0)2} \\ &\quad \times \exp \left(-2 \frac{\bar{x}^2 + \bar{y}^2}{w_{xy}^2} - 2 \frac{\bar{z}^2}{w_z^2} + 2i \xi \frac{n_1}{n_2} k_1 \bar{z} \right) \\ &\quad \times \exp \left[-ik_2 \left(z \cos \theta + y \sin \theta \sin \varphi + x \sin \theta \cos \varphi \right. \right. \\ &\quad \left. \left. + \frac{2\pi m}{Dk_2} \bar{z} + \frac{2\pi l}{Dk_2} \bar{y} \right) \right] dx dy dz\end{aligned}$$

By integration,¹⁹

$$\bar{E}_2(\theta, \varphi) = \sum_{m, l} C_w G_{ml} \bar{E}_2^{(0)} A(\theta, \varphi), \quad (9)$$

where we introduce the following parameters:

$$C_w = \left(\sqrt{\frac{\pi}{2}} \right)^3 w_{xy}^2 w_z C_v,$$

$$\bar{E}_2^{(0)} = \frac{\nu}{r} (\sin^2 \theta \sin^2 \varphi + \cos^2 \theta)^{1/2} \cdot \bar{\mu}_2^{(0)},$$

$$\bar{\mu}_2^{(0)} = \frac{1}{2} \bar{E}_1^2(0, 0, 0) \beta = \frac{1}{2} \bar{E}_1^{(0)2} \beta,$$

which represent the contribution from the local induced polarization per unit volume density to the radiated electric field at the focal center only [indicated by the superscript (0)],

$$\begin{aligned}A(\theta, \varphi) &= \exp \left\{ -\frac{k_2^2}{8} \left[w_{xy}^2 (\sin \theta \cos \varphi)^2 \right. \right. \\ &\quad \left. \left. + w_{xy}^2 \left(\sin \theta \sin \varphi + \frac{2\pi l}{Dk_2} \right)^2 \right. \right. \\ &\quad \left. \left. + w_z^2 \left(\cos \theta - \xi \frac{n_1}{n_2} + \frac{2\pi m}{Dk_2} \right)^2 \right] \right\}\end{aligned}$$

According to the phase-match condition in SHG, when a particular order of (m, l) for \bar{K}_{ml} achieves perfect phase match, it would be the only order that contributes to the buildup of SHG while contributions from all others are neglected as the oscillating terms. Hence, the integral symbol in Eq. (9) can be ignored to be

$$\bar{E}_2(\theta, \varphi) = C_w G_{ml} \bar{E}_2^{(0)} A(\theta, \varphi). \quad (10)$$

2.5 Emission Direction of Second Harmonic Generation Electric Field

SHG detected along the parallel (\parallel) and perpendicular (\perp) directions as the excitation polarization (α) are

$$\begin{aligned}\begin{pmatrix} \bar{E}_2^{\parallel} \\ \bar{E}_2^{\perp} \end{pmatrix} &= \begin{bmatrix} \cos(\varphi - \alpha) & -\sin(\varphi - \alpha) \\ \sin(\varphi - \alpha) & \cos(\varphi - \alpha) \end{bmatrix} \begin{pmatrix} \bar{E}_2^p \\ \bar{E}_2^s \end{pmatrix} \\ &= C_w G_{ml} A(\theta, \varphi) \begin{bmatrix} \cos(\varphi - \alpha) & -\sin(\varphi - \alpha) \\ \sin(\varphi - \alpha) & \cos(\varphi - \alpha) \end{bmatrix} \begin{pmatrix} \bar{E}_2^{(0)p} \\ \bar{E}_2^{(0)s} \end{pmatrix} \\ &= \frac{\nu}{r} C_w G_{ml} A(\theta, \varphi) \begin{bmatrix} \cos(\varphi - \alpha) & -\sin(\varphi - \alpha) \\ \sin(\varphi - \alpha) & \cos(\varphi - \alpha) \end{bmatrix} \cdot \bar{M} \cdot \bar{\mu}_2^{(0)},\end{aligned}$$

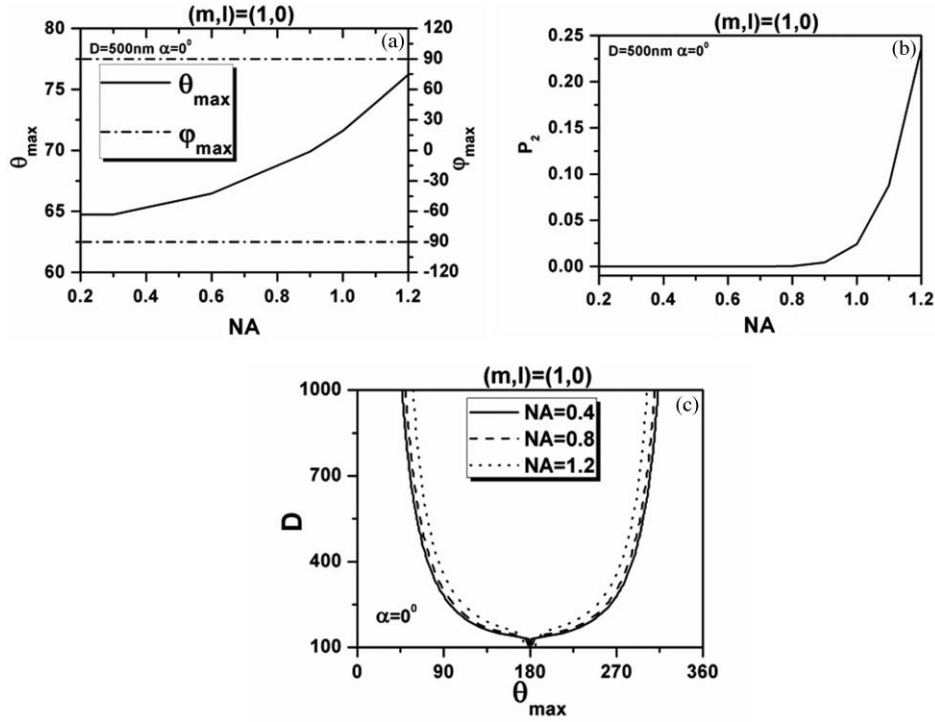


Fig. 2 (a) Peak SHG emission angle ($\theta_{\max}, \varphi_{\max}$) as the change of numerical aperture NA. (b) Effect of parameter NA on SHG emission power P_2 . (c) Peak SHG emission angle θ_{\max} varies as fibrils period D under different NA.

where \vec{M} is the projection matrix, which permutes coordinate (x, y, z) to (θ, φ) . It is defined by

$$\vec{M} \begin{pmatrix} \vec{\theta} \\ \vec{\varphi} \end{pmatrix} = \begin{pmatrix} \cos \theta \cos \varphi & \cos \theta \sin \varphi & -\sin \theta \\ -\sin \varphi & \cos \varphi & 0 \end{pmatrix}.$$

2.6 Second Harmonic Generation Emission Power

On the basis of the formula of electric field presented in Eq. (9), the total power distribution of SHG thus has the following expression:¹⁹

$$P_2(\theta, \varphi) = \frac{1}{8} n_2 \varepsilon_0 c v^2 \beta^2 \vec{E}_1^{(0)4} C_w^2 G_{ml}^2 H(\theta, \varphi), \quad (11)$$

where $H(\theta, \varphi) = A^2(\theta, \varphi) \cdot (1 - \sin^2 \theta \cos^2 \varphi)$.

The power distribution in parallel (\parallel) and perpendicular (\perp) components are

$$\begin{aligned} P_2^{\parallel}(\theta, \varphi) &= \frac{1}{2} n_2 \varepsilon_0 c r^2 |\vec{E}_{2\parallel}(\theta, \varphi)|^2 \\ &= \frac{1}{8} n_2 \varepsilon_0 c G_{ml}^2 v^2 C_w^2 A^2(\theta, \varphi) \vec{E}_1^{(0)4}, \end{aligned}$$

$$\begin{aligned} & \{ \cos(\varphi - \alpha) [\cos \theta \cos \varphi (\beta_{xxx} \cos^2 \alpha + \beta_{xyy} \sin^2 \alpha) \\ & + \beta_{xyy} \cos \theta \sin \varphi \sin 2\alpha] - \sin(\varphi - \alpha) \\ & \times [-\sin \varphi (\beta_{xxx} \cos^2 \alpha + \beta_{xyy} \sin^2 \alpha) \\ & + \beta_{xyy} \cos \varphi \sin 2\alpha] \}^2, \end{aligned} \quad (12)$$

$$\begin{aligned} P_2^{\perp}(\theta, \varphi) &= \frac{1}{2} n_2 \varepsilon_0 c r^2 |\vec{E}_2^{\perp}(\theta, \varphi)|^2 \\ &= \frac{1}{8} n_2 \varepsilon_0 c G_{ml}^2 v^2 C_w^2 A^2(\theta, \varphi) \vec{E}_1^{(0)4}, \end{aligned}$$

$$\begin{aligned} & \{ \sin(\varphi - \alpha) [\cos \theta \cos \varphi (\beta_{xxx} \cos^2 \alpha + \beta_{xyy} \sin^2 \alpha) \\ & + \beta_{xyy} \cos \theta \sin \varphi \sin 2\alpha] + \cos(\varphi - \alpha) \\ & \times [-\sin \varphi (\beta_{xxx} \cos^2 \alpha + \beta_{xyy} \sin^2 \alpha) \\ & + \beta_{xyy} \cos \varphi \sin 2\alpha] \}^2. \end{aligned} \quad (13)$$

3 Theoretical Simulation Study of Effects of Parameters on Second Harmonic Generation Emission Angle

In Eq. (11), $P_2(\theta, \varphi) \propto \beta^2$ indicates that the biophysical feature (denoted by β) of constituted collagen dipoles will only affect the total amount of SHG emission power rather than the power distribution along SHG emission angle (θ, φ) . In this paper, because we focus on the exploration of the parameters that may influence the SHG emission angle (θ, φ) , the effect of β is ignored and we make the following assumptions to simplify our model in this section. First, the ratio of the fibrils diameter to the collagen period is defined to be $R = d_1/D = 1/2$, which indicates the water interval d_2 has the same size with fibrils diameter $d_1 = (d_2 = d_1)$ as shown in Fig. 1(b). Second, a fixed value $\lambda_1 = 800$ nm is applied in our following simulations because, usually, the excitation wavelengths λ_1 that most experiments

take for SHG in biological applications are between 700 and 1000 nm. Third, the coefficient $(1/8)n_2\varepsilon_0c\nu^2E_1^{(0)4}$ is normalized to be 1.

3.1 Effects of Numerical Aperture on Second Harmonic Generation Emission Angle

Figure 2(a) demonstrates the peak SHG emission angle ($\theta_{\max}, \varphi_{\max}$) when the SHG emission power is maximum $P_{2\max}$, which implies the optimizing SHG imaging angle as NA changes from 0.2 to 1.2 under the condition of collagen period of $D = 500$ nm ($d_1 = 250$ nm), $(m, l) = (1, 0)$, and $\alpha = 0$ deg. We note that as NA increases from 0.2 to 1.2, θ_{\max} increases from 65 to 76 deg, while θ_{\max} always keeps in direction of $+90$ or -90 deg, indicating the emission direction of the maximum $P_{2\max}$ is confined in the yz plane when $\alpha = 0$ deg. NA has also been found to have influence on the total SHG emission power P_2 , as demonstrated in Fig. 2(b). It has a greater impact on P_2 within the range of 0.8–1.2 than that of 0.2–0.8, in which its influence is negligible. Hence, NA = 0.8 is chosen for our following discussions, where it is necessary. Figure 2(c) shows the variation of θ_{\max} with the collagen period D at NA 0.4, 0.8, and 1.2 under the order $(m, l) = (1, 0)$ and $\alpha = 0$ deg. It shows that all SHG emission has symmetrical characteristics that locate opposite the direction of the excitation light ($\theta = 180$ deg). Furthermore, we note that the influence of NA on θ_{\max} at different collagen period D does not make much difference. Compared to NA, collagen period D obviously has more of an impact on SHG emission angle θ_{\max} ; thus, it is explored in more detail in Sec. 3.3.

3.2 Effects of Structural Order (m, l) on Second Harmonic Generation Emission Angle

The 3-D distribution of SHG emission angles (θ, φ) under two collagen periods $D = 150$ nm ($d_1 = 75$ nm) and $D = 1000$ nm ($d_1 = 500$ nm) when $\alpha = 0$ deg with structural orders $(m, l) = (1, 0)$, $(0, 1)$, and $(1, 1)$, respectively, are demonstrated in Fig. 3. It shows that the peak emission angle φ_{\max} keeps the same value through all the orders and collagen periods, which is 90 deg and/or 270 deg (in the $\hat{y} - \hat{z}$ plane) under the excitation conditions. On the other hand, the peak emission angle θ_{\max} presents different patterns on D and (m, l) . We note that there are two emission lobes of SHG when $(m, l) = (1, 0)$, whereas at other demonstrated cases, only one emission lobe exists. Furthermore, we find that when $D = 1000$ nm, although under the case of $(m, l) = (1, 0)$, there are two SHG emission lobes, the emission power of these two lobes are much lower than that of $D = 150$ nm, which means, in practice, it could be undetectable. Also, under the structural order of $(m, l) = (0, 1)$ and $(m, l) = (1, 1)$, if the fibrils diameter D is smaller, such as $D = 150$ nm, then the only one emission lobe has much lower power to be detected.

The key point that attracts our attention in Fig. 3 is that when D is relatively smaller, such as $D = 150$ nm, under both $(m, l) = (1, 0)$ and $(1, 1)$, SHG emission presents the backward emission ($\theta_{\max} > 90$ deg). However, at $(m, l) = (0, 1)$, SHG emission presents the forward feature ($\theta_{\max} < 90$ deg). This result indicates that the structure character of collagen fiber along the incident light direction \vec{z} , which is characterized by the parameter m , plays the major role on backward emission of

SHG. When D is relatively bigger, for example, $D = 1000$ nm, SHG presents forward emission under all three (m, l) orders.

3.3 Effects of Collagen Period D on Second Harmonic Generation Emission Angle

Realizing that the collagen period D plays an important role on the peak SHG emission angle θ_{\max} , the impact of collagen period D from 100 to 1000 nm on the peak SHG emission angle under different orders $(1, 0)$, $(0, 1)$, and $(1, 1)$ in the case of NA = 0.8 and thus has correspondingly been demonstrated in Fig. 4(a). With the structural order $(1, 0)$ and $(1, 1)$, θ_{\max} drops dramatically from starting angle 180 deg at first and then decreases slowly after it crosses 90 deg (nonlinear). There is a threshold value of collagen period D , in our case it is ~ 300 nm. When D is smaller than this value, the backward emission of SHG occurs ($\theta_{\max} > 90$ deg); otherwise, SHG emits along the forward direction ($\theta_{\max} < 90$ deg). When the structural order (m, l) is $(0, 1)$, on the contrary, only two peak SHG emission angles denoting forward emission of either 26 deg ($D < 200$ nm) or 37 deg ($D \geq 200$ nm) along all sizes of D are induced. The variation of θ_{\max} as D is not smoothly, there is a quantum leap as shown in the inserted figure.

To further understand the functions of D on SHG emission, the effect of D on the total SHG emission power (P_2) under different cases of structural orders (m, l) are correspondingly shown in Fig. 4(b). Note that as the collagen period D is > 350 nm (relative larger size of D), the emission power of SHG under structural order $(0, 1)$ takes superior contribution over others to total SHG emission power. When $170 < D < 350$ nm (middle size of D), the emission power of SHG under structural order $(1, 1)$ plays dominant role. Although structural order $(1, 0)$ has its dominant contribution when the range of D falls between 100 and 170 nm. Figure 4(b) clearly demonstrates that the structural feature of collagen fiber [determined by structural order (m, l)] will play a role only on a certain range of collagen period D or fibrils diameter d_1 .

3.4 Effects of Polarization Angle α of Fundamental Light n Second Harmonic Generation Emission Angle

The effects of polarization angle α on peak SHG emission angles is taken into account, as shown in Fig. 5 [Eqs. (12) and (13)]. Here, the collagen period is assumed to be $D = 400$ nm and the first hyperpolarizabilities to be $\beta_{xyy} = 1$ and $\beta_{xxx} = 2.6$. Because the polarization angle α varies from 0 to π , we note that the peak angles (θ_s, θ_p) corresponding to the maximum perpendicular and parallel emission power keep stable values ($\theta_s = \theta_p$ is ~ 77 deg). While the peak angle φ_{\max} , on the other hand, has an obvious change. The peak angle φ_s corresponding to the maximum perpendicular SHG power increases with α and appears a distinct transit around $\alpha = 90$ deg. The peak angle φ_p corresponding to the maximum parallel SHG emission power almost keeps constant when α is between 50 and 130 deg. The changes of the emission angle as the polarization angle α have the same feature of quantum leap as that of φ_{\max} along D , as shown in Fig. 4(a).

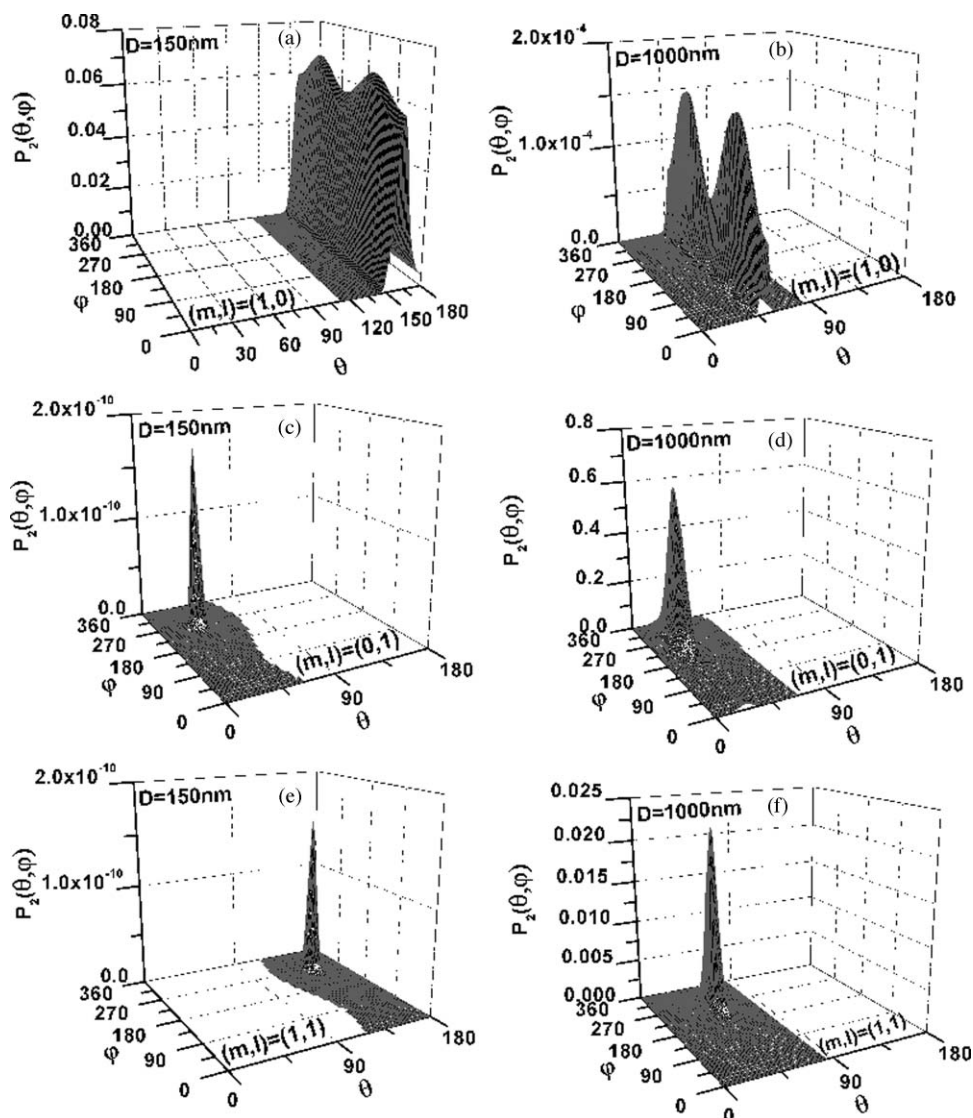


Fig. 3 SHG emission power distribution of (θ, φ) varies with two fibrils periods $D = 150\text{ nm}$ and $D = 1000\text{ nm}$ under the most commonly involved three structural orders $(m, l) = (1, 0)$, $(m, l) = (0, 1)$, and $(m, l) = (1, 1)$.

4 Conclusions and Discussions

According to the structural characteristics of collagen type I fiber, which is constituted by fibrils in a square quasi-crystalline formation, the density distribution function $C(x, y, z)$ describing the distribution of dipoles in such crystallized fibrils bundle and structural order (m, l) characterized by QPM theory is introduced in this paper to deal with the SHG emission from collagen fiber. The effects of NA, structural order (m, l) , collagen period $D = d_1 + d_2$, as well as polarization angle α on emission angles of SHG have been investigated.

NA has influence on SHG emission angle, such as the increase of NA causes an increase of the peak emission angle θ_{\max} and the total SHG emission power, but for different D , the difference is slight.

We have made a detailed investigation of collagen period D on SHG emission in this paper. Because $D = d_1 + d_2$, to utilize the results to get an intuitive understanding of the fibrils diameter d_1 on SHG emission, we assume that $d_1 = D/2$ here. This assumption is reasonable if we are only interested in the effects

of d_1 on the SHG emission angle. The ratio of fibrils diameter to collagen period ($R = d_1/D$), without a doubt, has an influence on G_{ml} , as shown in Fig. 6. However, based on Eq. (9), we know that G_{ml} would only affect the total amount power of SHG rather than the emission angle and the corresponding power distribution. Therefore, $d_1 = D/2$ ($R = 1/2$) is made when we analyze the effect of d_1 on θ_{\max} based on the results of D . Our investigations show that, when the diameter of fibrils d_1 decreases, for the same structural order, for example, $(m, l) = (1, 0)$ or $(1, 1)$ and at the same NA, the θ_{\max} increases correspondingly. As the diameter of fibrils d_1 reaches a threshold value, which in our case is around $d_1 = 150\text{ nm}$, backward SHG emission appears [Fig. 4(a)]. The relationship of forward/backward emission of SHG with the fibril's diameter has been supported by previous experimental results. It has been shown that there are more striking SHG backward images than the forward from fibril segments of immature two-day-old rat-tail tendon,¹⁶ which is predominated by immature fibrils (small diameter of fibrils⁸). Also, in 10-day-old rat-tail tendon, they verify that

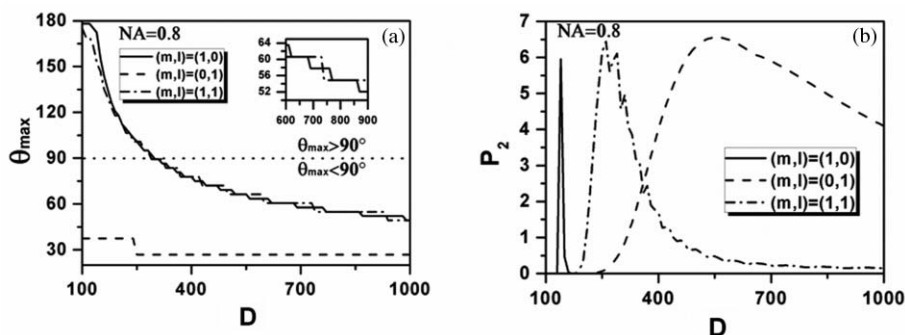


Fig. 4 (a) Effect of fibrils period D at different (m,l) on peak SHG emission angle θ_{\max} . (b) SHG total emission power as varied fibrils period D at different (m,l) .

the immature fibril segments scatter backward, whereas mature fibril segments (the large diameter of fibrils⁸) is forward.²⁴ Our simulation results of SHG backward emission has been further verified by the experimental results of forward to backward (F/B) ratio of SHG to fibril diameter.¹⁶ There, the diameter of fibrils is modulated by the NaCl concentration; the higher of the NaCl concentration is, the smaller the fibrils size is due to shrinkage. The experimental results clearly show that the F/B ratio obviously decrease with the decrease of fibril size induced by an increase of NaCl concentrations.

Our simulation results regarding the effects of structural order (m,l) indicate that the structural feature of collagen fiber along the incident light direction \bar{z} , which is characterized by the parameter m , plays a major role on backward emission of SHG because the fibril diameter is small enough (Fig. 3), where $(m,l) = (1,0)$ and $(1,1)$ makes the backward SHG emission happen when $D = 150$ nm; however, $(m,l) = (0,1)$ makes SHG emission keep the forward direction. Furthermore, Fig. 4 shows that θ_{\max} has little difference between structural order $(1,0)$ and $(1,1)$ as the variation of D , which also indicates that, compared to m,l , has a minor effect on the determination of θ_{\max} . In other words, the structure feature along the incident light direction has the dominant effect on θ_{\max} to be forward or backward.

Additionally, the simulation results demonstrated in Figs. 3 and 4(b) indicate that, under the certain structural features represented by (m,l) , such as $(m,l) = (1,0)$, there are two symmetrical emission lobes along all the collagen periods D (Fig. 3).

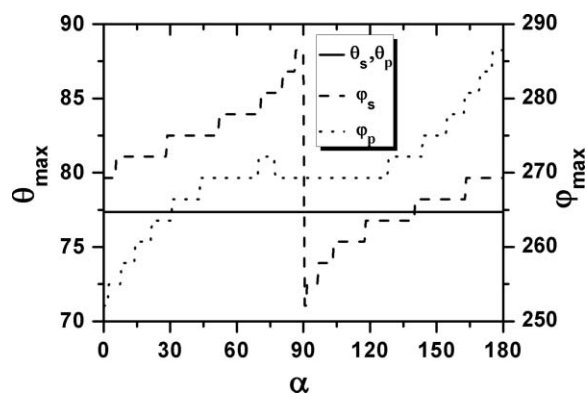


Fig. 5 Peak SHG emission angle (θ,φ) , in perpendicular and parallel direction, change with the polarization angle α .

However, if this structural feature does not function on those collagen periods D , here, for example, $D = 1000$ nm, which is out of the scope (100–170 nm), where the structural order $(m,l) = (1,0)$ has its dominant contribution [Fig. 4(b)], the emission power produced from the collagen fiber with those collagen periods would be very low; the two emission lobes appear theoretically would not exist in practice [Figs. 3(b) and 3(c)]. In other circumstances, such that the collagen fiber satisfies the structural feature of $(m,l) = (0,1)$ or $(m,l) = (1,1)$, it is possible to have only one emission lobe of SHG [Figs. 3(c)–3(f)]. However, Fig. 4(b) indicates that if the collagen fiber period D falls in the range of the overlapping functional area of $(m,l) = (0,1)$ and $(1,1)$, both structural features may have their contributions to the SHG emission; therefore, two SHG emission lobes would still be expected, but the emission power of those two lobes could be unbalanced.

From our simulation results in Fig. 5, we realize that fundamental wave polarization angle α has no influence on θ_{\max} but on φ_{\max} . Our theoretical simulation results of the optimizing SHG imaging angle $(\theta_{\max},\varphi_{\max})$ with the relationship of the NA, collagen structure order (m,l) , fibrils diameter d_1 , and the polarization angle α of the incident laser would be very helpful on the optimization of experimental protocols for efficient SHG imaging.

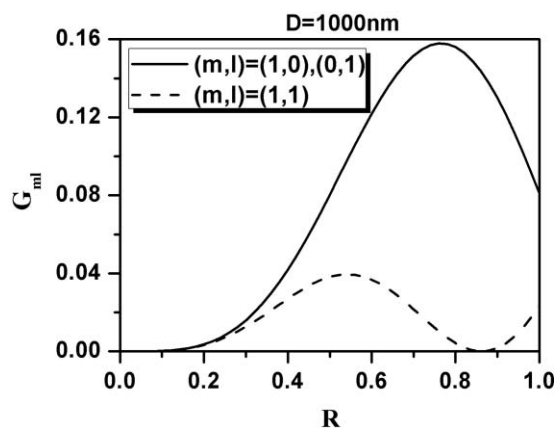


Fig. 6 C_{ml} varies as ratio of fibrils diameter to collagen period ($R = d_1/D$) at different (m,l) .

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