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**Abstract.** This communication describes some details of polarization modulation that are useful in phase-shifting interferometry when applied to phase profile measurements of phase objects. Since non-destructive optical techniques allow surface measurement with high accuracy, a Mach-Zehnder configuration coupled to a 4-f arrangement using phase gratings placed on the Fourier plane was implemented to analyze phase objects. Each beam of the interferometer goes through a birefringent wave plate in order to achieve nearly circular polarization of opposite rotations, with respect to each other. The interference of the fields associated with replicated beams, centered on each diffraction order, is achieved varying the spacing of windows with respect to the grating period. Experimental results are presented for cases of four and nine simultaneously captured interferograms. © 2012 Society of Photo-Optical Instrumentation Engineers (SPIE). [DOI: 10.1117/1.OE.51.5.055601]

Subject terms: phase shifting; interferometry; phase objects; phase grating.

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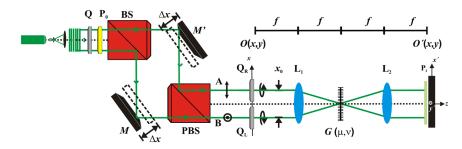
#### 1 Introduction

In this work, we propose a configuration of a two-window polarizing phase shifting interferometer, 1,2 based on two coupled systems: a Mach-Zehnder interferometer (MZI) that allows the two-window generation with adjustable separation, and a 4-f system with Phase gratings placed on the frequency plane; 3,4 due to that, the change in beam separation can be freely adjusted. One advantage is that, when beam separation is properly changed, interference of the different diffractions orders can be obtained. The system is insensitive to external vibrations itself due to its quasicommon path configuration. The previously presented two-window interferometer with diffraction grating<sup>3</sup> was implemented using a fixed separation exclusively designed for the grid used; in the proposed configuration, we can freely adjust these separation and positions. Also, with the proposed optical system, we can obtain results of the same quality as those obtained in previous reports, in a more flexible system which is not limited by optical components, such as the grid used. The MZI system, unlike a system based on a Sagnac triangular, has the advantage of being adapted for use in other applications, such as microscopy (placing a microscopic system on one arm) or phase shifting optical tomography (by obtaining parallel projections for each angle of rotation of the transparent sample); the aforementioned applications are considered future work of the research proposed in this report.

To generate independent phase shifts in the interference patterns, a linear polarizer is placed at a convenient angle on each replica.<sup>5</sup> In the experimental results presented, the Interference patterns are processed by means of two methods, for the case of four interferograms and in the case of nine interferograms, using the symmetrical (N + 1) nine algorithms.<sup>6,7</sup>

#### 2 Experimental Setup

The optical system proposed is shown in Fig. 1. It consists of a combination of a quarter-wave plate Q and a linear polarizing filter  $P_0$  that generates linearly polarized light oriented



**Fig. 1** Experimental setup. BS: Beamsplitter PBS: polarizing beamsplitter O(x,y): object plane O'(x,y): image plane  $L_i$ : lens  $G(\mu,\nu)$ : phase grid  $P_i$ : polarizer's grating period d=110 lines/mm  $x_0=10$  mm f=150 mm a'=1.519 rad. The transparent sample is collocated on B.

at a 45-deg angle entering the Mach Zehnder configuration from a YVO<sub>3</sub> laser operating at 532 nm (see Fig. 1). This configuration generates two symmetrically displaced beams by moving mirrors M and M' enabling one to change spacing  $x_0$  between beam centers. Two retardation plates ( $Q_L$ and  $Q_R$ ), with mutually orthogonal fast axes, are placed in front of the two beams (A, B) to generate left and r ight nearly-circular polarized light.<sup>8,9</sup> A phase-grating  $G(u/\lambda f, v/\lambda f)$  is placed on the frequency plane (u, v) of the 4-f Fourier optical system that is coupled to the MZI configuration, with f being the focal length of each transforming lens. Then,  $\mu = u/\lambda f$  and  $v = v/\lambda f$  are the frequency coordinates scaled to wavelength  $\lambda$  and the focal length. On plane  $(\mu, \nu)$ , the period of G is denoted by d, and its spatial frequency by  $\sigma = 1/d$ . Two neighboring diffraction orders have a distance of  $X_0 \equiv \lambda f/d$  at the image plane for a grating; then,  $\sigma \cdot u = X_0 \cdot \mu$  and  $X_0$  can be used as a frequency. In the following sections, phase shifts caused by the grating at the image plane of this system are discussed.

#### 3 Phase Grating Interferometry

Phase gratings have interesting properties, as well as the advantage of using a higher percentage of incident energy than absorption gratings. In this report, we use crossphase gratings, with the advantage of being able to generate up to 16 replicas of the interferogram with independent phase shifts; this allows the use of other algorithms to process phase. Furthermore, the use of cross-phase gratings allows one to obtain  $\pi$ -phase shifts, simplifying the polarizer arrangement. It is known from Ref. 10 that the retardation error generated by the wave plates and the phase aberration of the diffractive elements can be neglected, the intensity aberration of diffractive wavefronts, and pixel mismatch should be corrected.  $^{10}$  One should select good optical

elements, such as high efficiency gratings, imaging lens and detectors. A phase grid, carefully constructed by means of superposing two phase gratings with their respective grating vectors at  $\pm 90$  deg, is placed at the system's Fourier planes. Taking the rulings of one grating along the  $\mu = u/\lambda f$  direction and the rulings of the second grating along the  $v = v/\lambda f$  direction, the resulting centered phase grid can be written as

$$G(\mu, v) = e^{i2\pi A_g \sin[2\pi \cdot X_0 \mu]} e^{i2\pi A_g \sin[2\pi \cdot X_0 \nu]}$$

$$= \sum_{q=-\infty}^{\infty} J_q(2\pi A_g) e^{i2\pi \cdot qX_0 \mu} \sum_{r=-\infty}^{\infty} J_r(2\pi A_g) e^{i2\pi \cdot rX_0 \nu}, (1)$$

where the frequencies along each axis direction are taken as  $X_0$ , with  $2\pi Ag$  being the phase grating amplitude, and  $J_q$  and  $J_r$  the Bessel functions of the first kind of integer order q, r, respectively. The Fourier transform of the phase grid becomes

$$\tilde{G}(x,y) = \sum_{q=-\infty}^{q=\infty} \sum_{r=-\infty}^{r=\infty} J_q(2\pi A_g) J_r(2\pi A_g) \delta(x - qX_0, y - rX_0),$$
(2)

which consists of point-like diffraction orders distributed on the image plane.

#### 3.1 Interference-Pattern Contrasts and Modulation

Phase grid interferometry is based on a two crossed phase grating placed as the pupil in a 4-f Fourier optical system. A convenient window pair for a grating interferometer implies an amplitude transmittance given by

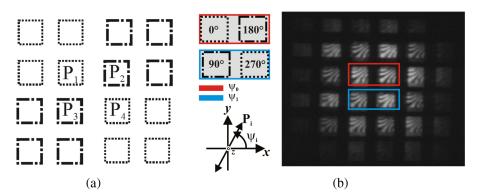
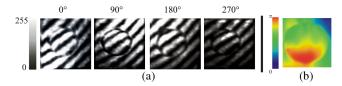


Fig. 2 Replicas of the interference patterns obtained with the phase grid. (a) Polarizing filters array and (b) experimental interference patterns.



**Fig. 3** Phase dot prepared evaporating magnesium fluoride  $(MgF_2)$  on a glass substrate. (a) Four 90 deg phase-shifted interferograms and (b) phase profile.

$$O(x, y) = A\left(x + \frac{x_0}{2}, y\right) + B\left(x - \frac{x_0}{2}, y\right),$$
 (3)

where  $x_0$  is the separation from center to center between two beams, A(x, y) as the reference beam aperture and B(x, y) is the beam aperture where the phase object is placed. Placing a grating of spatial period  $d = \lambda f/F_0$  at the Fourier plane, with a corresponding transmittance given by  $G(\mu, v)$ . The image formed by the system consists basically of replications of each window at distances  $F_0$ . This image is defined by O'(x, y); that is, the convolution of O(x, y) with the Fourier transform of the phase grating,  $\tilde{G}(x, y)$  represented by

$$O'(x, y) = O(x, y) * \tilde{G}(x, y)$$

$$= w \left( x + \frac{x_0}{2}, y \right) * \sum_{q = -\infty}^{\infty} J_q(2\pi A_g) \delta(x - qF_0, y)$$

$$+ \left[ w \left( x - \frac{x_0}{2}, y \right) e^{i\phi(x - \frac{x_0}{2}, y)} \right]$$

$$* \sum_{q = -\infty}^{\infty} J_q(2\pi A_g) \delta(x - qF_0, y), \tag{4}$$

where (\*) denotes the convolution. By adding the terms of Eq. (4), taking q and q-1 (both located within the same replicated window  $w(x-qF_0+\frac{x_0}{2},y)$ ), and for the case of matching the beams's positions with the diffraction order's positions ( $F_0=x_0$ ), the previous equation simplifies to

$$O'(x,y) = \sum_{q=-\infty}^{\infty} \left[ J_q(2\pi A_g) + J_{q-1}(2\pi A_g) e^{i\phi(x-x_0[q-\frac{1}{2}],y)} \right]$$

$$w \left[ x - x_0 \left( q - \frac{1}{2} \right), y \right]. \tag{5}$$

Thus, an interference pattern between fields associated to each window must appear within each replicated window. The fringe modulation  $m_q$  of each pattern would be of the form

$$m_q = \frac{2J_q J_{q-1}}{J_q^2 + J_{q-1}^2},\tag{6}$$

where each fringe contrast depends on the relative phases between the Bessel functions  $J_q$ .

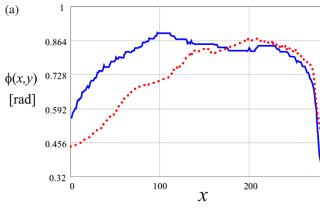
## **3.2** Phase Shifting Interferometry with Modulation of Polarization

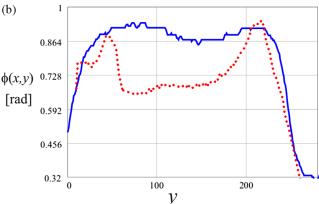
Turning the attention to gratings, in order to introduce additional phase shifts in the interference pattern centered around  $(x_0[q-(1/2)], y)$ , each of the windows is illuminated with

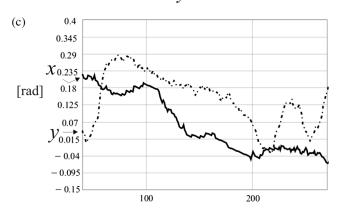
different polarizations using retarding plates  $Q_R$  and  $Q_L$  (Fig. 1); this arrangement introduces Jones polarization vectors  $\vec{J}_R$  and  $\vec{J}_L$  into the interference terms of Eq. (4). After placing a linear polarizing filter with the transmission axis at an angle  $\psi$ , its irradiance turns out to be proportional to

$$\|\vec{J}_T\|^2 = A(\xi, \alpha') \{ (J_q^2 + J_{q-1}^2) + 2J_q J_{q-1} \cos[\xi(\psi, \alpha') - \phi(x, y)] \},$$
 (7)

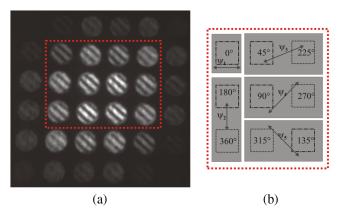
where  $\vec{J}_T = J_{\psi}^l \vec{J}_L J_q + J_{\psi}^l \vec{J}_R J_{q-1}$ ,  $J_{\psi}^l$  is the transmission matrix for the linear polarizer at angle  $\psi$ ,  $\pm \alpha'$  is the retardation of each plate, and  $\xi(\psi, \alpha')$  denotes the phase shifting term induced by modulation of polarization given by







**Fig. 4** Continued line: Phases along typical raster lines of phase dot of Fig. 3; Dotted line: Phases along typical raster lines of phase dot of Ref. 1; (a) Traze along-*x*, (b) traze along-*y*, and (c) plot of differences along the two directions.



**Fig. 5** Interference patterns detected with a polarizing filter at  $\psi=25$  deg. (a) The interference patterns used are enclosed in the dotted rectangle and (b) polarizer filter array for N=8, nine symmetrical interferograms.

 $\xi(\psi,\alpha')$ 

$$= \operatorname{Arc} \operatorname{Tan} \left[ \frac{\sin[2\psi] \cdot \sin[\alpha'] + \sin^2[\psi] \cdot \sin[2\alpha']}{\cos^2[\psi] + \sin^2[\psi] \cdot \cos[2\alpha'] + \sin[2\psi] \cdot \cos[\alpha']} \right];$$
(8)

 $A(\psi, \alpha')$  is defined as

$$A(\psi, \alpha') = 1 + \sin[2\psi]\cos[\alpha'] \tag{9}$$

denoting each pattern as

$$\|\vec{J}_i\|^2 = A(\xi, \alpha')\{(J_q^2 + J_{q-1}^2) + 2J_{\alpha}J_{\alpha-1}\cos[\xi(\psi_i, \alpha') - \phi(x, y)]\}$$
(10)

with  $i = 1 \dots N$ .

#### 3.2.1 Case of four interferograms

For phase-shifting interferometry with four patterns, four irradiances can be used, each one taken at a different  $\psi$  angle. The relative phase can be calculated by Refs. 6 and 11

$$\tan \phi = \frac{\|\vec{J}_1\|^2 - \|\vec{J}_3\|^2}{\|\vec{J}_2\|^2 - \|\vec{J}_4\|^2},\tag{11}$$

where  $\|\vec{J}_1\|^2$ ,  $\|\vec{J}_2\|^2$ ,  $\|\vec{J}_3\|^2$  and  $\|\vec{J}_4\|^2$  are the intensity measurements with the values of  $\psi$  such that  $\xi(\psi_1)=0$ ,  $\xi(\psi_2)=\pi/2$ ,  $\xi(\psi_3)=\pi$ ,  $\xi(\psi_4)=3\pi/2$ , respectively. Note that  $\xi(\psi,\pi/2)=2\psi$  and  $A(\psi,\pi/2)=1$ , so a good choice for the retarders is quarter-wave retarders, as it is well known. Dependence of  $\phi$  on the coordinates of the centered point has been simplified to x, y. The same fringe modulation  $m_q$  results as in Eq. (6). Therefore, the discussion about fringe modulation given in previous sections is retained when introducing the modulation of polarization. Such polarization modulation can be carried out also for grids, resulting in similar conclusions.

#### 3.2.2 Case of nine interferograms

To demonstrate the use of the various interferograms obtained to extract phase under the conditions described above, we choose the symmetrical N+1 phase steps algorithms for data processing, the phase is given by Ref. 7:

$$\tan \phi(x, y) = \frac{\sum_{i}^{N+1} I_{i} \sin(2\pi \frac{i-1}{N})}{\sum_{i}^{N+1} I_{i} \cos(2\pi \frac{i-1}{N})},$$
(12)

where N+1 is the number of interferograms. For the case of nine interferograms, only five linear polarizing filters have to be placed. The transmission axes of the filter pairs  $P_1$  can be the same for each one, as long as they cover two patterns with  $\pi$ -phase shift in between.

#### 3.3 Phase Shifts

Experimentally, the phase shifting obtained is the result of placing a linear polarizer in each one of the interference patterns generated on each diffracting orders on the exit plane  $(P_i)$ ; each polarizing filter transmission axis is adjusted at a different angle  $\psi_i$ , see Fig. 2(a). The experimental observations suggest a simplification for the polarizing filter array due to the  $\pi$  phase shift obtained; thus, it is not necessary to use all linear polarizing filters for all patterns. For example, in the case of four steps, we only need to place two polarizers ( $P_0$  and  $P_1$ ), each one covering two patterns with complementary phase shifts; then,  $\psi_0 = 0$  deg and  $\psi_1 = 46.557 \text{ deg},^2$  which leads to phase shifts  $\xi$  of 0, 0,  $\pi/2$ ,  $\pi$ , and  $3\pi/2$ , and can be seen in Fig. 2(b), with the dotted boxes representing the polarizing filters. This result allows us to know the phase profile. Since *n*-interferograms can be obtained simultaneously, the dynamic study of a phase objects can be carried out.

#### 3.4 Phase Objects

If placed on B arm of the interferometer, a transparent object (without absorption) can be expressed as:

$$O(x, y) = e^{i \cdot \phi(x, y)},\tag{13}$$

where  $\phi(x, y)$  is a real function; this object is known as a phase object. Consider the special case where  $|\phi(x, y)|^2 \ll 1$ , resulting in the kind of transparent objects known as thin phase objects we obtain

$$O(x, y) = 1 + i \cdot \phi(x, y); \tag{14}$$

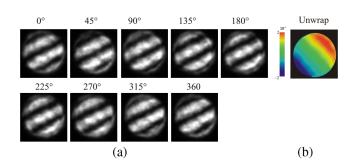


Fig. 6 Tilted wavefront. (a) Nine 45 deg phase-shifted interferograms and (b) unwrapped phase data map.

with i being a constant, maintaining a constant phase relationship  $\pi/2$  because  $i=e^{i\cdot\pi/2}$ . Equation (4) allows us to retrieve the phase profile of the transparent sample. The phase reconstruction is performed using Eqs. (11) or (12), according to the case.

### 4 Experimental Results: Static and Dynamic Distributions

The phase gratings that were used are the commercially available ones. (Edmund Optics' transmission grating, dimensions:  $25 \times 25$  mm; dimensional tolerance:  $\pm 0.5$  mm; substrate: Optical Crown Glass). The monochromatic camera used is based on a CMOS sensor with  $1280 \times 1024$  pixels and with a pixel pitch of  $6.7 \mu m$ . Each interferogram was typically composed of arrays of 600 × 512 pixels, and filtered with a conventional low-pass filter to remove sharp edges and detail from the image, leaving smooth gradients and low-frequency detail. To reduce differences of irradiance and fringe modulation, each interferogram used was subjected to a rescaling and normalized process. This procedure generates patterns of equal background and equal fringe modulation. There are several two-dimensional (2-D) phase unwrapping algorithms; however, for simplicity, the method used for unwrapping the phase data was a non-iterative fast cosine method. 12

#### 4.1 Static Distributions: Four Interferograms Case

A phase dot generated with a magnesium fluoride film  $(MgF_2)$  on a glass substrate, was placed in the path of beam B, while beam A was used as a reference; the results obtained are shown in Fig. 3. Figure 3(a) shows the four patterns with  $\pi/2$  phase shifts obtained in a single shot, and Fig. 3(b) presents the phase profile of the object, in

false color coding. More than four interferograms could be used, whether for N-steps phase-shifting interferometry or for averaging images with the same shift. Figure 4 presents the comparative case, between the measurements of the phase dot, measured with a two window interferometer with the measurement made with the proposed system. Figure 4(a) shows cross sections along the axis x, and Fig. 4(b) shows cross sections along the axis y. Variations which increase near the edges can be observed between the two measures, and are due to processing of the interferograms. The results presented in Ref. 1 show the interferograms were not filtering as evidenced by speckle noise, which leads to errors in the unwrapped phase. This can be seen on the graph of the differences along the two directions in Fig. 4(c).

The difference presented in the results obtained, which were compared with Ref. 1, is caused mostly by object deterioration. In the results presented, the fringe patterns obtained correspond to changes in the curvature surface.

Comparatively, the results obtained with the proposed optical system are equal to those obtained with an interferometer double-fixed window, however, the implementation of this optical system becomes simpler since it is easier to place the necessary components. Also, we are able to use phase grids with other periods, or absorption grids, only taking in consideration the correct separation of the two windows.

The accuracy in measurements is the one typical of phase-shifting. Some trade-offs appear while placing several images over the same detector field, but for low frequencies interferograms (with respect to the inverse of the pixel spacing) the influence of these factors seems to be rather small if noticeable.

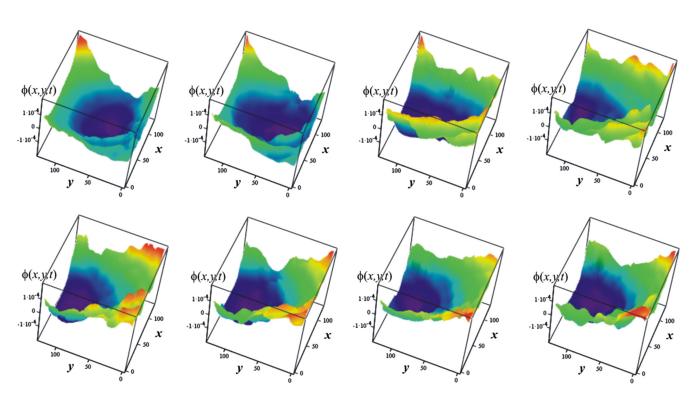


Fig. 7 Dynamics distributions; representative frames; evolution of the phase profile, one capture per 2 sec (Video 1, QuickTime, MOV, 725 KB) [URL: http://dx.doi.org/10.1117/1.OE.51.5.055601.1].

#### **4.2** Static Distributions: Case of Nine Interferograms

To demonstrate the use of several interferograms, we choose the symmetrical n = (N + 1) phase steps algorithms, <sup>7</sup> for data processing (case N = 8). A constant phase shift value of  $2\pi/N$  is employed when using these techniques. The phase shifts of  $\pi$  due to the grid spectra allow the use of a number of polarizing filters that is less than the number of interferograms, simplifying the filter array (see Fig. 5). According to Fig. 5(b), it can be shown that for a symmetrical nine,  $\psi_1 = 0$ ,  $\psi_2 = 92.989$ ,  $\psi_3 = 22.975$ ,  $\psi_4 = 46.577$ , and  $\psi_5 = 157.903$  deg. In this case, each resulting step  $\xi$  corresponds to a 45-deg phaseshift.<sup>2</sup> The corresponding results and calculated phases are shown in Fig. 6. The experimental results show the interference pattern and unwrapped phase generated by a tilted wavefront. This system is capable of obtaining n = N + 1interferograms in a single capture.

#### 4.3 Dynamic Distributions

A dynamic phase object is shown in Fig. 7 (Video 1). It corresponds to flowing oil on a glass microscope slide allowing to flow under the effect of gravity. The phase object was put in front of B windows of the system of Fig. 1. For this case, four interferograms are used to process the optical phase.

The figure shows the temporal evolution of the oil flow (Video 1). The oil drop is deformed due to the action of gravity during the observation period. With better control of the parameters of the experiment we can calculate the fluid velocity, and that is a future work of the techniques presented. One of the advantages of phase-shift systems is that they allow simultaneous observation of dynamic events.

#### 5 Conclusions

The experimental set-up for an adjustable two-window interferometer based in a Mach Zehnder configuration has been described to obtain the phase profile of phase objects from the analysis of optical phase using polarizing phase shifting techniques. This system is able to obtain Ninterferograms with only one shot  $(n \le 16)$ .

Tests with four phase-shifts were presented, but we also tested other approaches using different phase-shifts attained by using linear polarizers with their transmission axes at the proper angle before detection (case of nine interferograms). The phase shifts of  $\pi$  due to the grid spectra allows the use of a number of polarizing filters which is less than the number of interferograms, simplifying the filter array. The interferometric system allows the analysis of static objects and dynamics objects.

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